

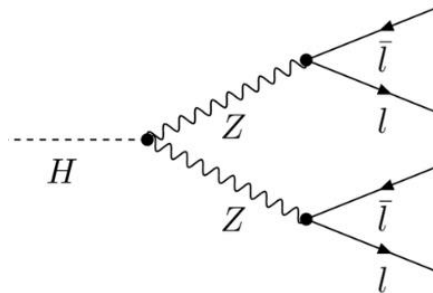
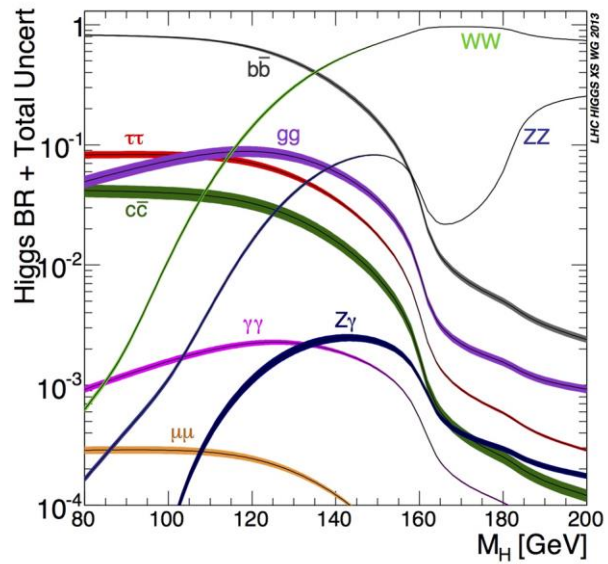
Muon Resolution Studies for the Higgs Mass Measurement

Alex Wen

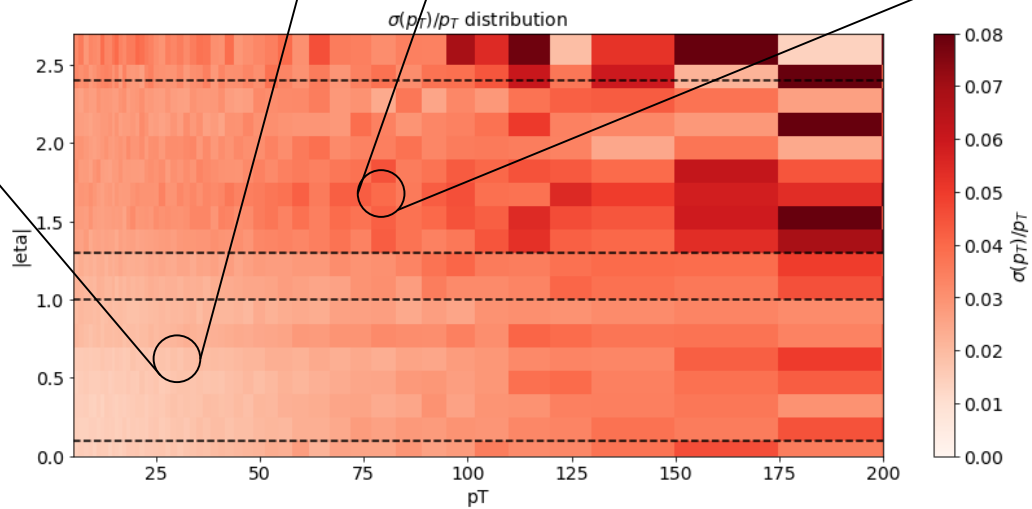
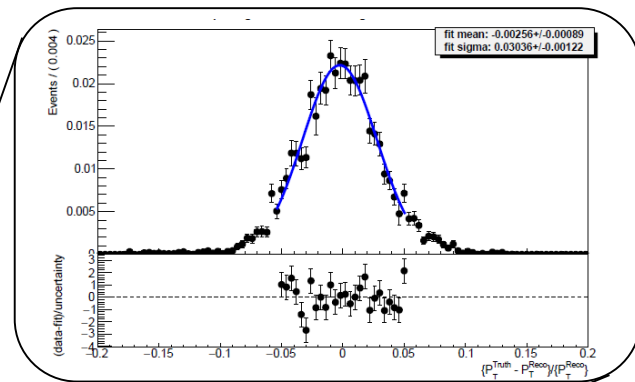
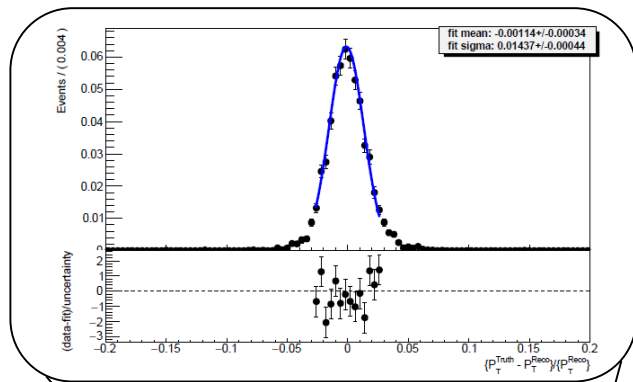
ATLAS Canada Summer Student Presentations
August 20, 2020

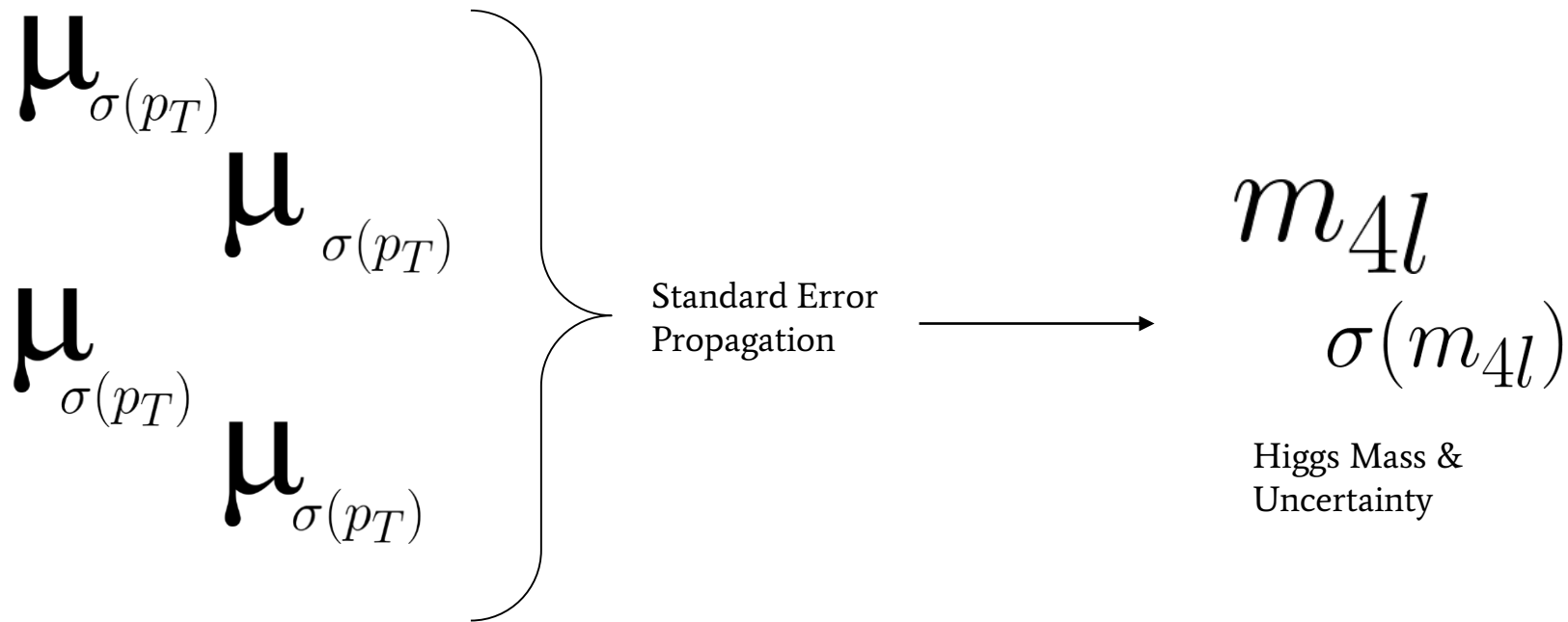
People: Pierre Savard (Supervisor), Lukas Adamek
ATLAS Group @ University of Toronto





Method





μ
 μ μ
 μ μ

$$m_{4l}^2 = \left(\sum_i E_i \right)^2 - \left| \sum_i \vec{p}_i \right|^2 \approx \left(\sum_i p_i \right)^2 - \left| \sum_i \vec{p}_i \right|^2$$

$$m_{4l}^2 = \sum_{i \neq j} (p_i p_j - \vec{p}_i \cdot \vec{p}_j)$$

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 μ μ
 μ μ

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$$m_{4l}^2 = \sum_{i \neq j} (p_i p_j - \vec{p}_i \cdot \vec{p}_j)$$

$$p_x = p_T \cos(\phi), \quad p_y = p_T \sin(\phi), \quad p_z = p_T \sinh(\eta)$$

$$|\vec{p}| = p_T \sqrt{\cos^2(\phi) + \sin^2(\phi) + \sinh^2(\eta)} = p_T \cosh(\eta)$$

μ
 μ
 μ

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$$m_{4l}^2 = \sum_{i \neq j} p_{T,i} p_{T,j} (\cosh(\eta_i - \eta_j) - \cos(\phi_i - \phi_j))$$

μ
 μ μ
 μ

$$m_{4l}^2 = \left(\sum_i E_i \right)^2 - \left| \sum_i \vec{p}_i \right|^2 \approx \left(\sum_i p_i \right)^2 - \left| \sum_i \vec{p}_i \right|^2$$

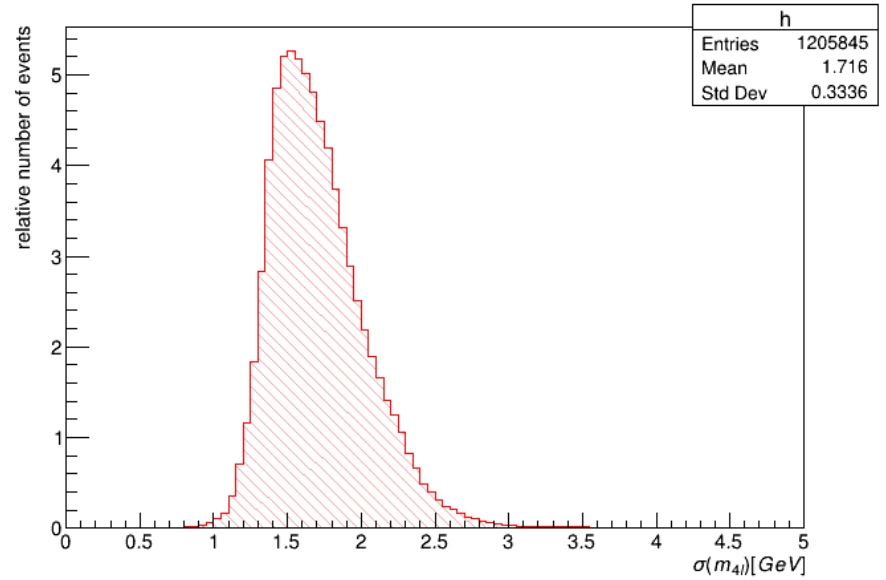
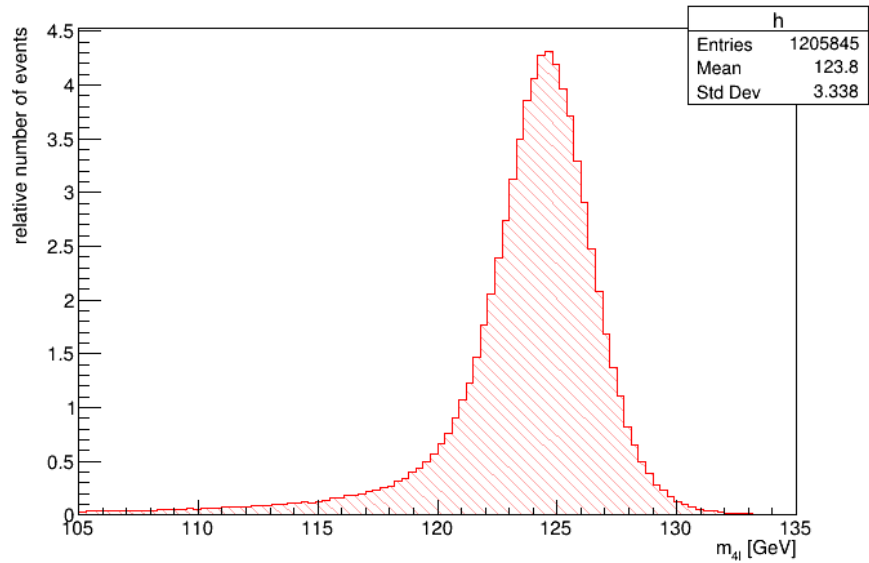
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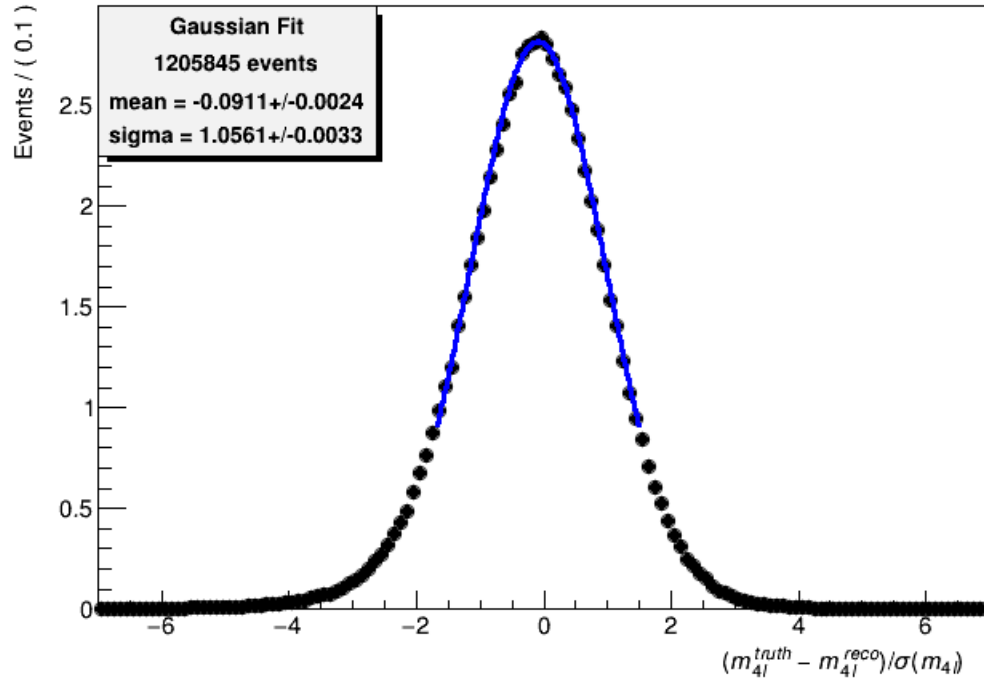
$$|\vec{p}| = p_T \sqrt{\cos^2(\phi) + \sin^2(\phi) + \sinh^2(\eta)} = p_T \cosh(\eta)$$

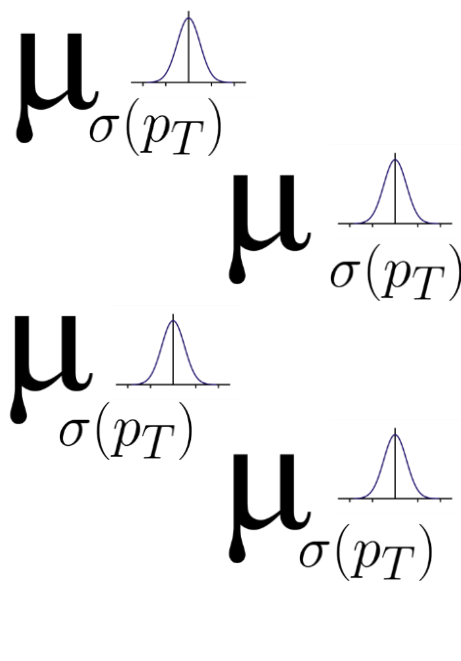
$$m_{4l}^2 = \sum_{i \neq j} p_{T,i} p_{T,j} (\cosh(\eta_i - \eta_j) - \cos(\phi_i - \phi_j))$$

$$\sigma(m_{4l}^2) = \sqrt{\sum_i \left(\frac{\partial(m_{4l}^2)}{\partial p_{T,i}} \sigma(p_{T,i}) \right)^2}$$

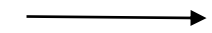


Pulls

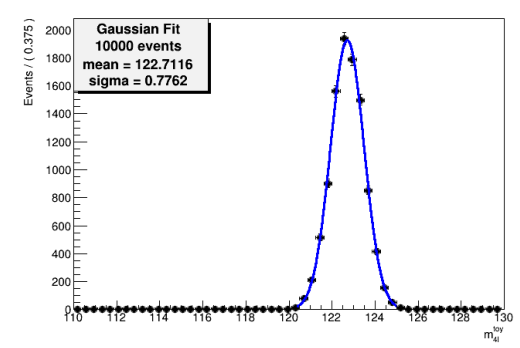




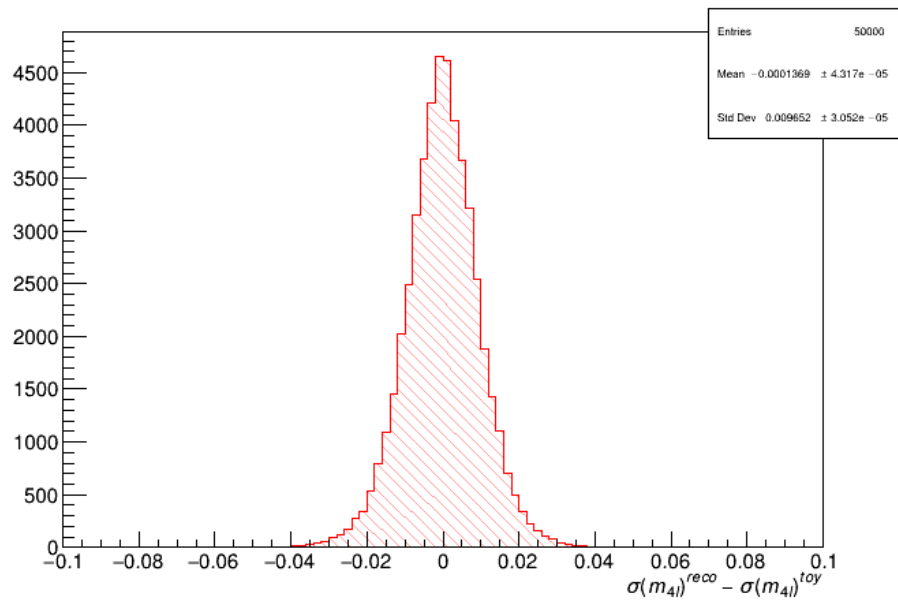
Sample many times



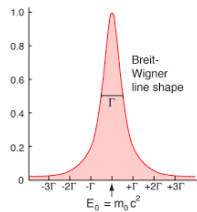
m_{4l} distribution



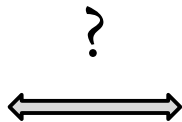
Higgs Mass & Uncertainty



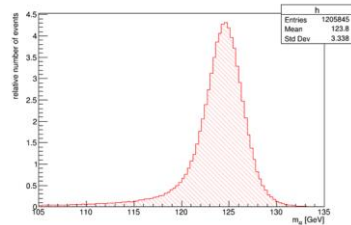
Mass Measurement



True mass value m_H

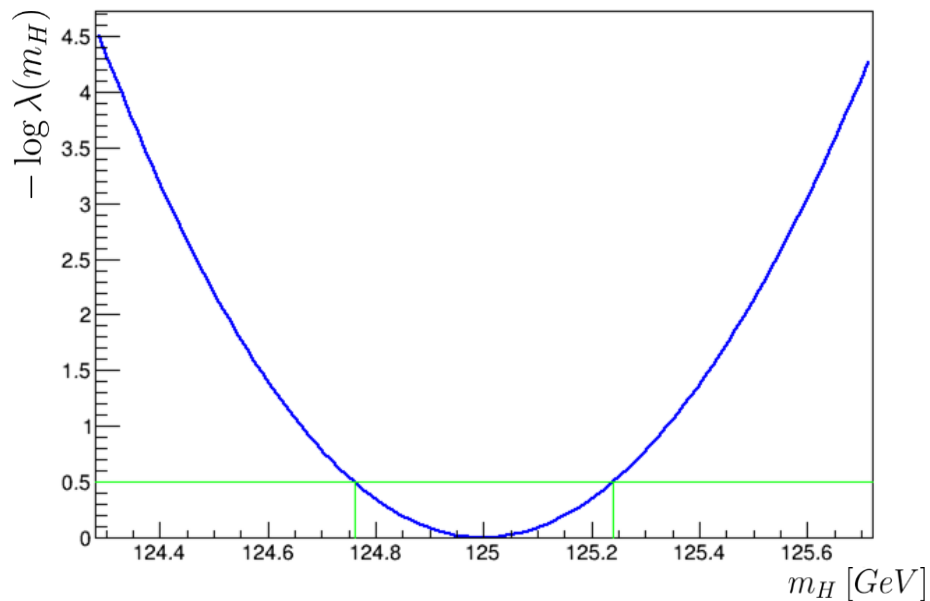


The mean of the resultant mass distribution (a double crystal ball)



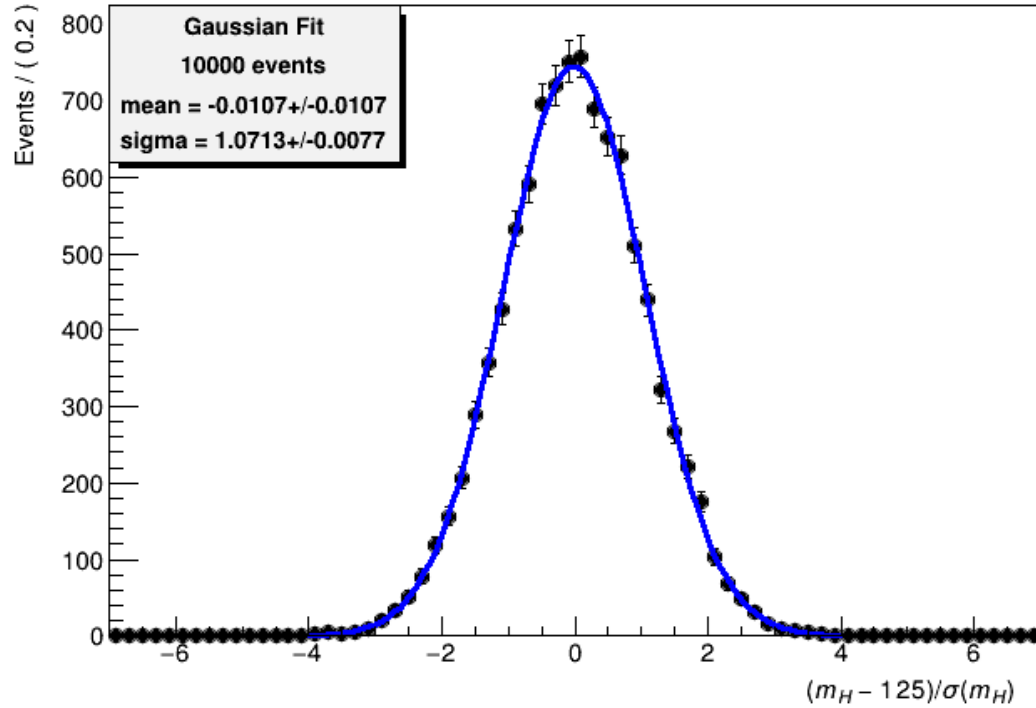
$$\text{mean} = a(m_H - 125) + b$$

Maximize the profile likelihood ratio λ with respect to m_H on, say, 125 GeV MC



$$125.00^{+0.24}_{-0.24} \text{ GeV}$$

Pulls



Summary:

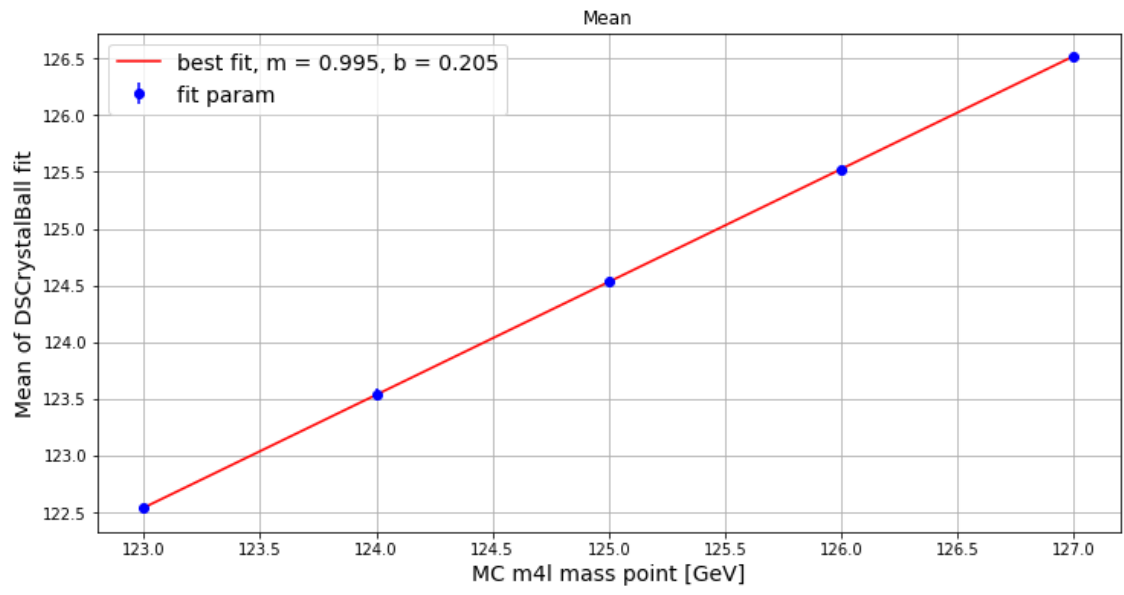
- We have a simple, robust, and valid way of estimating per-event mass resolution
- We are still working on a model that improves the final mass resolution

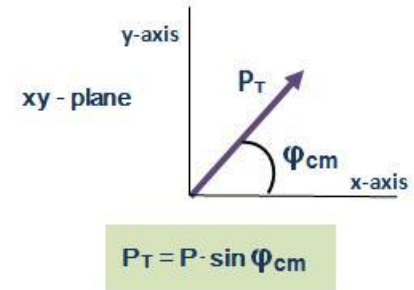
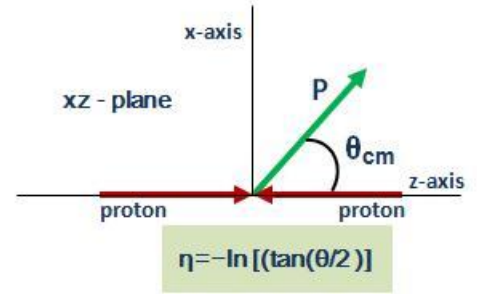
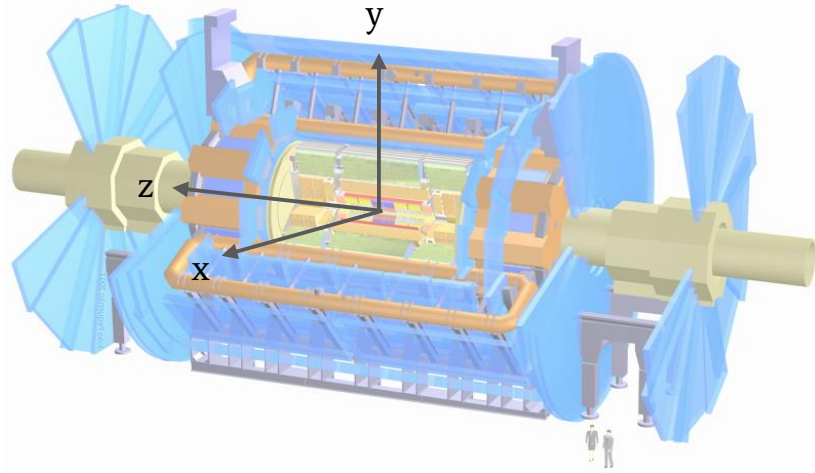
$$125.00^{+0.24}_{-0.24} \text{ GeV}$$

Thanks!



Backup





Current Approach

Assume we have muons 1, 2, 3, 4.

Assuming a negligible mass and therefore $E \approx p$,

$$m_{4l}^2 = (E_1 + E_2 + E_3 + E_4)^2 - (\vec{p}_1 + \vec{p}_2 + \vec{p}_3 + \vec{p}_4)^2 \approx (p_1 + p_2 + p_3 + p_4)^2 - (\vec{p}_1 + \vec{p}_2 + \vec{p}_3 + \vec{p}_4)^2$$

Expanding, cancelling terms, and rewriting the terms,

$$m_{4l}^2 = 2(p_1 p_2 - \vec{p}_1 \cdot \vec{p}_1) + 2(p_1 p_3 - \vec{p}_1 \cdot \vec{p}_3) + 2(p_1 p_4 - \vec{p}_1 \cdot \vec{p}_4) + 2(p_2 p_3 - \vec{p}_2 \cdot \vec{p}_3) + 2(p_2 p_4 - \vec{p}_2 \cdot \vec{p}_4) + 2(p_3 p_4 - \vec{p}_3 \cdot \vec{p}_4)$$

Defining $F(i, j) = (p_i p_j - \vec{p}_i \cdot \vec{p}_j)$ and using the identities

- $p_x = p_T \cos(\phi)$
- $p_y = p_T \sin(\phi)$
- $p_z = p_T \sinh(\eta)$
- $p = p_T \sqrt{\cos^2(\phi) + \sin^2(\phi) + \sinh^2(\eta)} = p_T \sqrt{1 + \sinh^2(\eta)} = p_T \cosh(\eta)$

we obtain

$$F(i, j) = p_{T,i} p_{T,j} (\cosh(\eta_i) \cosh(\eta_j) - \cos(\phi_i) \cos(\phi_j) - \sin(\phi_i) \sin(\phi_j) - \sinh(\eta_i) \sinh(\eta_j))$$

which simplifies to

$$F(i, j) = p_{T,i} p_{T,j} (\cosh(\eta_i - \eta_j) - \cos(\phi_i - \phi_j))$$

Therefore, we can write

$$m_{4l}^2 = 2(F(1, 2) + F(1, 3) + F(1, 4) + F(2, 3) + F(2, 4) + F(3, 4))$$

Finally, it is a simple procedure to take the square root to get

$$m_{4l} = \sqrt{m_{4l}^2}$$

$$DCB(m_{4\ell}; \mu, \sigma, \alpha_1, n_1, \alpha_2, n_2) = C \begin{cases} \left(\frac{n_1}{\alpha_1}\right)^{n_1} \cdot e^{-\frac{\alpha_1^2}{2}} \cdot \left(\frac{n_1}{\alpha_1} - \alpha_1 - \frac{m_{4\ell} - \mu}{\sigma}\right)^{-n_1}, & \left(\frac{m_{4\ell} - \mu}{\sigma}\right) < -\alpha_1 \\ e^{-0.5 \frac{(m_{4\ell} - \mu)^2}{\sigma^2}}, & -\alpha_1 \leq \left(\frac{m_{4\ell} - \mu}{\sigma}\right) \leq \alpha_2 \\ \left(\frac{n_2}{\alpha_2}\right)^{n_2} \cdot e^{-\frac{\alpha_2^2}{2}} \cdot \left(\frac{n_2}{\alpha_2} - \alpha_2 + \frac{m_{4\ell} - \mu}{\sigma}\right)^{-n_2}, & \alpha_2 < \left(\frac{m_{4\ell} - \mu}{\sigma}\right) \end{cases}$$

$$\lambda(m_H) = \frac{L(m_H, \hat{\theta}(m_H))}{L(\hat{m}_H, \hat{\theta})},$$